

High-Level, First-Principles, Full-Dimensional Quantum Calculation of the Ro-vibrational Spectrum of the Simplest Criegee Intermediate (CH₂OO)

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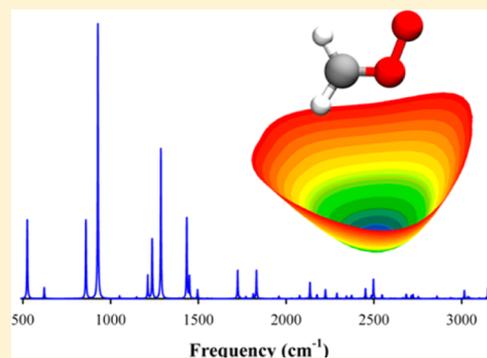
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ABSTRACT: The ro-vibrational spectrum of the simplest Criegee intermediate (CH₂OO) has been determined quantum mechanically based on nine-dimensional potential energy and dipole surfaces for its ground electronic state. The potential energy surface is fitted to more than 50 000 high-level ab initio points with a root-mean-square error of 25 cm⁻¹, using a recently proposed permutation invariant polynomial neural network method. The calculated rotational constants, vibrational frequencies, and spectral intensities of CH₂OO are in excellent agreement with experiment. The potential energy surface provides a valuable platform for studying highly excited vibrational and unimolecular reaction dynamics of this important molecule.



SECTION: Environmental and Atmospheric Chemistry, Aerosol Processes, Geochemistry, and Astrochemistry

Ozonolysis,¹ namely, the reactions of ozone with alkenes from either natural or man-made sources including combustion, is an important atmospheric process, leading to free radicals such as OH. The mechanism of ozonolysis is believed to start with an exothermic 1,3-cycloaddition of O₃ to the C=C double bond, leading to a primary ozonide (POZ). Predicted by Criegee in 1949, the dissociation of POZ produces an important intermediate, namely R₁R₂COO with R₁,R₂=H/alkyl bonded directly to C.² Despite their importance, it is only recently that the Criegee intermediates have started to be directly detected and investigated in the gas phase,^{3,4} thanks to an efficient scheme to generate such metastable species.⁵ Due to the exothermic nature of the reaction, the Criegee intermediates are often produced with large amounts of internal energy and are thus highly reactive with short lifetimes. It is now established that they are involved in several important atmospheric reactions with unexpectedly rapid rates,^{5–9} but can be removed via photodissociation near 340 nm, leading to O(¹D) and aldehydes/ketones.^{10–14} As a result, they are now considered as major initiators of oxidation reactions in the atmosphere, in addition to the hydroxyl radical, particularly in winter when the photoproduction of OH is inefficient.^{1,3}

To elucidate the chemical and photochemical reactions involving the Criegee intermediates, it is imperative to understand their structures as well as the vibrational and unimolecular reaction dynamics in their ground electronic states. Indeed, the simplest Criegee intermediate (CH₂OO or

formaldehyde oxide) has been argued to exist in either a biradical¹⁵ or zwitterionic form,^{16,17} which have different structural and reaction characteristics. So far, the structure of CH₂OO has been determined experimentally using microwave spectroscopy,^{18–20} and its vibrational spectrum has been recorded with infrared (IR) spectroscopy.²¹ Theoretical models are essential in assigning the spectroscopic features in these experiments.

The recent flurry of spectroscopic measurements has posed a challenge to theory to better understand the structure and dynamics of this important molecule. Although some ab initio calculations of CH₂OO have been reported and vibrational frequencies computed,^{16,19,21–24} there has been no global potential energy surface (PES) that will allow a thorough understanding of not only its highly excited vibrational states, but also isomerization and decomposition dynamics. The only theoretical study of such unimolecular processes was done using a direct-dynamics method.²⁵ In this Letter, we report the first nine-dimensional PES for CH₂OO based on ~50 000 high-level ab initio points. These points were fit with the recently proposed permutation invariant polynomial neural network (PIP-NN) method,^{26,27} with a root-mean square error (RMSE) of only 3.1 meV (25 cm⁻¹). Anharmonic vibrational energy

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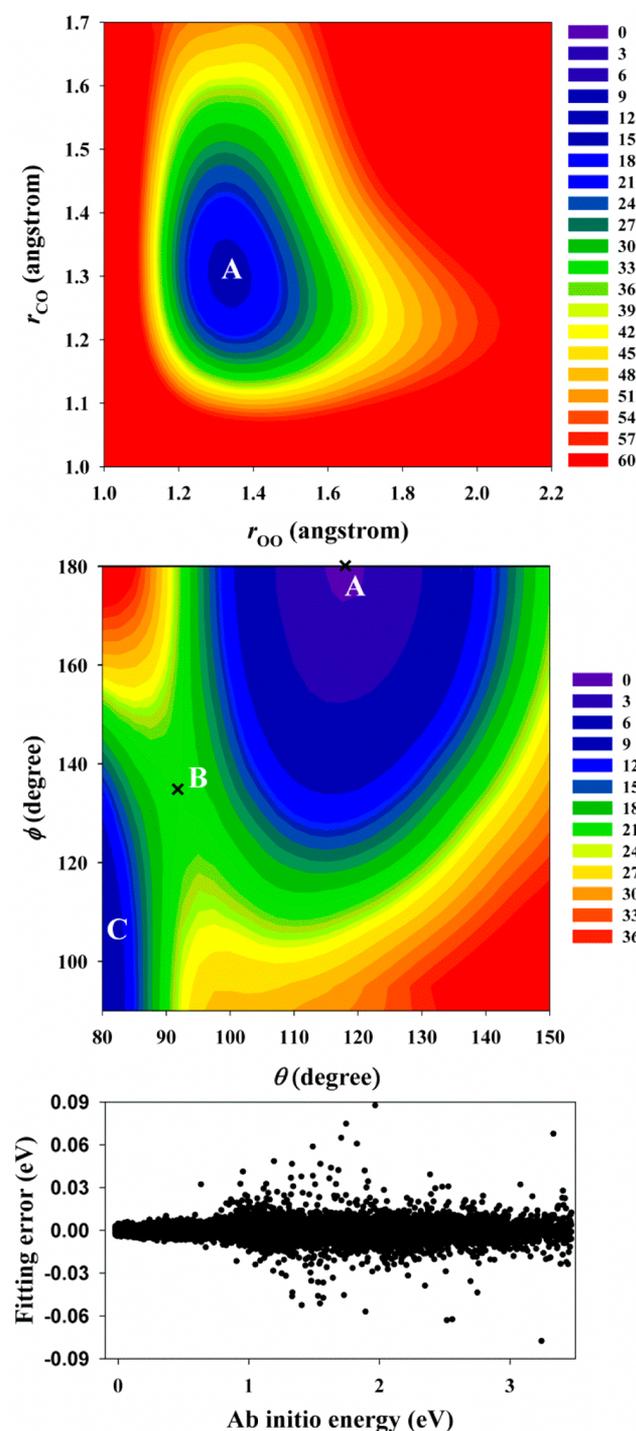


Figure 2. (a) Contour plots along the bond lengths O–O (x -axis) and C–O (y -axis), other coordinates optimized within a plane. (b) Contour plots along the COO bond angle (x -axis) and the HCOO dihedral angle (y -axis) with other coordinates optimized. (c) Fitting errors ($E_{\text{fit}} - E_{\text{ab}}$, in eV) as a function of the ab initio energies (in eV). Energies in (a) and (b) are in kcal/mol. A and C denote the potential minima for CH_2OO and its cyclic isomer dioxirane, with B as the transition state (TS1).

frequencies are listed in Table 1 with previous experimental and theoretical data.

In order to provide an accurate PES with reasonable computational costs, it is vital to choose the distribution of the ab initio points prudently. Following our earlier

strategies,^{32–34} we first determined a set of geometries near the CH_2OO equilibrium by running direct-dynamics trajectories (in particular, the Atomic Centered Density Matrix Propagation molecular dynamics model implemented in Gaussian 09³⁵ was employed) at the B3LYP/6-31+G(d, p) level. These geometries were screened to remove points that are too close to each other, using the Euclidean criteria $\chi = (\sum_i^{10} (r_i - r_i^{\text{new}})^2)^{1/2} < 0.1 \text{ \AA}$ where r_i is the internuclear distance. Although CH_2OO has several decomposition and isomerization channels, configurations far from its equilibrium geometry are excluded in this work. Note that due to the permutation symmetry, each configuration actually corresponds to four sets of internuclear distances, and all are considered in the screening. The CCSD(T)-F12a/AVTZ calculations were then carried out and the results were fit to a primitive PES. To further explore the topography of the PES, batches of classical trajectories with different energies were run, and additional geometries were chosen using the same protocol described above. This procedure was iterated multiple times until the results were converged.

In total, 50 459 points were calculated. The PES was constructed with the PIP-NN method,^{26,27} which has shown excellent performance in fitting PESs for several 4- and 5-atom systems.^{27,36–38} Briefly, the input layer of the NN consists of low-order PIPs, which are symmetrized monomials,³⁹

$$\mathbf{G} = \hat{\mathbf{S}} \prod_{i < j}^N p_{ij}^{l_{ij}} \quad (1)$$

where $p_{ij} = \exp(-ar_{ij})$ are the Morse-like variables with a as an adjustable constant and r_{ij} the $N(N - 1)/2$ (here $N = 5$) internuclear distances.³² l_{ij} is the degree of p_{ij} and $M = \sum_{i < j}^N l_{ij}$ is the total degree in each monomial. $\hat{\mathbf{S}}$ is the symmetrization operator, which consists of all possible nuclear permutation operations in the system. This direct symmetrization has been developed previously, without NN fitting, by Bowman and co-workers.³² It is worth noting that the number of PIPs in the input layer should be sufficiently large to ensure the permutation symmetry of the system.²⁷ For this system, we have included all 101 PIPs up to third order.

The explicit form of the basis functions in the neurons can be found in refs 26–27 and thus are not repeated here. Several different NN structures with one or two hidden layers were tested. We settled on two hidden layers with N_1 and N_2 neurons, respectively. In each NN fitting, the data were divided randomly into three sets, namely the training (90% of the data points), validation (5%), and test (5%) sets. All NN fittings were performed using the Levenberg–Marquardt algorithm with the following root-mean-square error (RMSE):

$$\text{RMSE} = \sqrt{\sum_{i=1}^{N_{\text{data}}} w(E_i^{\text{output}} - E_i^{\text{target}})^2 / N_{\text{data}}} \quad (2)$$

where w is the weighting function that assigns a factor of 5 for energy points below 0.8 eV while unity for others, and E_i^{target} and E_i^{output} are the input and fitted energies, respectively. To avoid false extrapolation due to edge points in the randomly selected validation and test sets, only fits with similar RMSEs for all three sets were accepted. In addition, the maximum deviation is also used in selecting the final PIP-NN fits. For each architecture, 50 different training calculations were performed, and the “early stopping” method⁴⁰ was used to avoid over fitting. The training method converges quickly for all

Table 2. Pure Rotational Transition Frequencies between Different $J_{K_a K_c}$ States (in cm^{-1}) of CH_2OO

$1_{01}-0_{00}$		$2_{02}-1_{01}$		$1_{10}-1_{01}$		$1_{11}-2_{02}$	
expt. ^a	theo. ^b						
0.7734	0.7721	1.5457	1.5432	2.2357	2.2291	0.6319	0.6127

^aExperiment.¹⁸ ^bThis work, theoretical calculations.

Table 3. Rotational Constants for Several Isotopomers of CH_2OO

	A_0		B_0		C_0	
	expt. ^a	theo. ^b	expt. ^a	theo. ^b	expt. ^a	theo. ^b
H_2COO	2.5934	2.6005	0.4158	0.4182	0.3576	0.3603
$\text{H}_2^{13}\text{COO}$	2.5709	2.5777	0.4033	0.4056	0.3479	0.3505
$\text{H}_2\text{C}^{18}\text{OO}$	2.4482	2.4537	0.4158	0.4181	0.3547	0.3573
$\text{H}_2\text{CO}^{18}\text{O}$	2.5646	2.5715	0.3928	0.3951	0.3400	0.3425
D_2COO	2.0191	2.0257	0.3693	0.3712	0.3116	0.3137
$d_{1,\text{trans}}\text{-HDCCO}$	2.5563	2.5639	0.3773	0.3794	0.3282	0.3305
$d_{1,\text{cis}}\text{-HDCCO}$	2.0604	2.0672	0.4048	0.4069	0.3376	0.3400
$\text{D}_2\text{C}^{18}\text{O}^{18}\text{O}$	1.9026	1.9081	0.3491	0.3508	0.2944	0.2963
$\text{H}_2\text{C}^{18}\text{O}^{18}\text{O}$	2.4180	2.4234	0.3926	0.3948	0.3371	0.3395

^aReference 19, while other experimental numbers^{18,20} are very close. ^bThis work, theoretical calculations, computed from the same minimum structure.

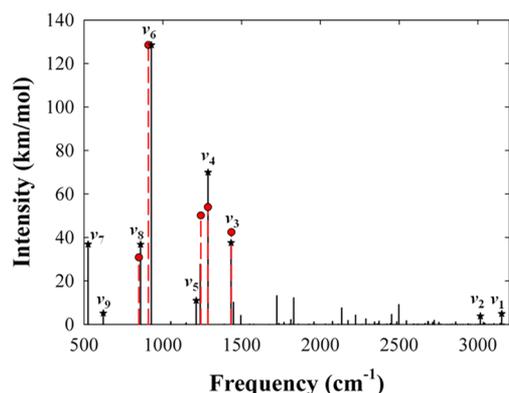


Figure 3. Comparison of the IR spectrum of CH_2OO obtained from experiment²¹ (in dashed red) and theory (in solid black), in which the experimental values are normalized with the intensity of the ν_6 line. The fundamentals are all indicated with additional symbols (circles or stars for experiment or theory).

the fitting reported here, typically finishing within a few hundred steps. The final PIP-NN PES was chosen as the average of three best fits.

The final fits have a NN structure of 10 and 40 interconnected neurons in the two hidden layers with 1501 parameters and the three best PIP-NN fits have RMSEs for train/valid/test sets and the maximum deviation of 3.8/4.4/6.0/197.8, 4.0/4.5/5.2/111.3, and 3.2/4.6/5.5/188.8 meV, respectively. The RMSE of the averaged PIP-NN PES is 3.1 meV, and the maximum deviation is 87.6 meV. The ab initio equilibrium geometry and harmonic frequencies are well reproduced by the PES, as shown in Figure 1 and Table 1. In Figure 2, contour plots are displayed in two pairs of coordinates. In panel a, the potential minimum is clearly seen, and the elongation of the O–O or C–O bonds eventually leads the O + CH_2O or CH_2 + O_2 dissociation limit. In panel b, the potential rises steeply along the dihedral angle (ϕ), consistent with a C=O double bond. In addition, the transition state (TS1) between formaldehyde oxide (CH_2OO) and the cyclic

dioxirane (CH_2O_2) is clearly seen. Finally, the fitting errors of all the data points are shown in panel c of the same figure.

The permanent dipole of CH_2OO was computed to be 4.11 D at the CCSD(T)-F12a/AVDZ level, comparable to 3.97 D calculated at a similar level by Cremer et al.¹⁶ A total of 45743 points in the CH_2OO well were computed and fit to a point-charge expression using the PIP method.⁴¹ 1122 parameters were used for each component of the dipole moment, and the RMSEs of the fits are 0.027, 0.007, and 0.003 D for the x , y , z components, respectively. Note that the dipole moment is related to the coordinate origin, and all the sampled points were in the principal axis frame.

The ro-vibrational energy levels of CH_2OO on this new PES were determined using the MULTIMODE approach²⁸ based on the Watson Hamiltonian.⁴² Since it has been discussed extensively in the literature, few details are given here. It suffices to say that mass-scaled normal mode coordinates are used in the Hamiltonian. The vibrational wave function is written as an expansion of direct-product basis functions, while the potential is expanded with a hierarchical n -mode representation. The calculations were done with a truncated potential with up to 6-mode terms. The $J = 0$ vibrational problem was first solved using the vibrational self-consistent field (VSCF) approach.^{43,44} To account for coupling among the nine vibrational modes, we go beyond the VSCF approximation by expanding the vibrational wave function in terms of the eigenfunctions of the VSCF Hamiltonian. This virtual configuration interaction (VCI) method^{45,46} typically improves the results, and is used here with up to 5-mode excitations. Convergence tests suggest that the vibrational frequencies are converged to $\sim 2 \text{ cm}^{-1}$. For $J > 0$, the basis for the VCI calculations is a direct product of the VSCF basis and symmetric top wave functions $|JKO\rangle$, and the ro-vibrational levels are obtained by diagonalization of the corresponding Hamiltonian matrix.⁴⁶ The intensities were computed using the method described in ref 47.

In Table 1, the $J = 0$ calculated VCI anharmonic vibrational frequencies on the PES are compared with both experimental and previous theoretical values. The agreement with the experimental data of Su et al.²¹ is quite satisfactory. We note

that the experimental value for the ν_5 (CH_2 rock) mode (1241 cm^{-1}) is possibly misassigned, and a new value is expected to be smaller (Y.-P. Lee, private communication), and thus closer to our prediction. The only large error is found for the O–O stretching frequency, which corresponds to the asymmetric stretching mode of the isoelectronic O_3 . The asymmetric stretching frequency in ozone is challenging to calculate accurately and is sensitive to higher-order electron correlation. MRCI(Q)/CBS overshoots ν_3 by roughly 30 cm^{-1} while still underestimating D_e . Higher-order correlation is needed to soften the well, yet increase D_e .^{48–50} Watts and Bartlett found that for single reference coupled cluster methods the effect of adding triple excitations contributed changes in the harmonic stretching frequency ω_3 (ozone) of more than 100 cm^{-1} , a dramatic effect of high-order correlation.⁵¹ Given the similarities to the complicated electronic structure of ozone, we consider the performance of the CCSD(T)-F12a/AVTZ method to be remarkably good for CH_2OO .

Calculated pure rotational excitation frequencies for the ground vibrational state of CH_2OO are compared in Table 2 with available experimental data.¹⁸ The agreement is quite satisfactory. In Table 3, the calculated rotational constants for several isotopomers of CH_2OO are listed along with the values derived from measurements.^{18–20} Again, the agreement is excellent.

In Figure 3, the calculated IR spectrum for CH_2OO is displayed, with comparison with the experimental spectral positions and relative intensities. The latter was normalized with the ν_6 feature. It is clear that the agreement is quite satisfactory. It should be noted that the experimental spectrum is restricted to a region between 800 and 1500 cm^{-1} . As a result, some strong features predicted by our calculations have not been observed, thus serving as predictions. In addition, the calculated ν_5 feature has a much smaller intensity than reported by the experiment, which supports the notion that this line might have been misassigned. As shown in the figure, the experimental frequency (1241 cm^{-1}) is very close to a relatively strong feature in the calculated spectrum, which was assigned to be $2\nu_9$ (1237 cm^{-1}), which borrows some intensity from ν_4 through mode mixing.

To summarize, we have constructed a full nine-dimensional highly accurate semiglobal PES for the simplest Criegee intermediate (CH_2OO) and the dipole surface. They allowed us to determine the vibrational spectrum and rotational constants. Agreement with the available experimental data is generally excellent, and the theoretical predictions are expected to help sort out the assignment of the experimental spectral features. This PES will also provide a solid foundation for further studies of the highly excited vibrational spectrum as well as unimolecular and photochemical reactions in this important system.

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Notes

The authors declare no competing financial interest.

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